On optimal decision-making in brains and social insect colonies

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Overview

- Goals
- Decision making
- Ants and Bees house hunting
- Models
- Discussion

Goals

- Compare a model of primate decision-making to 3 different models of house hunting by social insect colonies.
- Determine whether such models can implement or approximate the statistically optimal strategy given for primates.
- Make steps towards a common theoretical framework for the study of decision-making in biological systems.

Decision-making

Decision-making

A process where uncertain information must be processed to make a choice between two or more alternatives.

Optimal decision-making

Pareto inefficiency

Pareto inefficiency

Pareto Inefficiency

C

Quantity of Butter Produced

Pareto efficiency

Pareto efficiency

Inefficiency

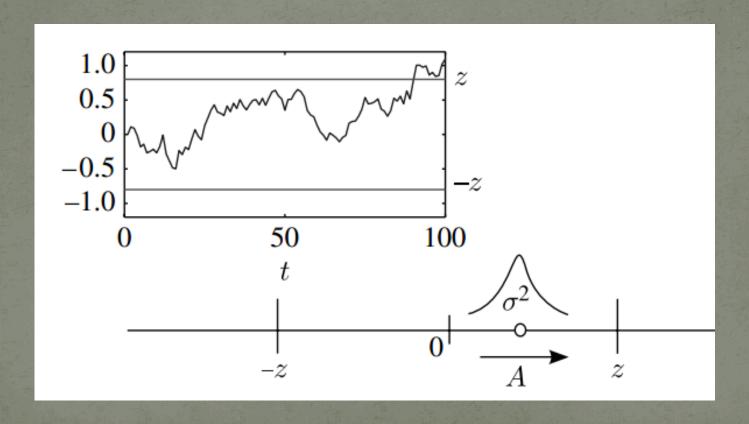
Source: http://upload.wikimedia.org/wikipedia/commons/b/bd/ Production_Possibilities_Pareto_Curve.png

Diffusion Model

- SPRT (sequential probability ratio test)
- Can be represented abstractly as Brownian motion
- 31-d Browning Motion Example
- Drunken walk

Diffusion Model

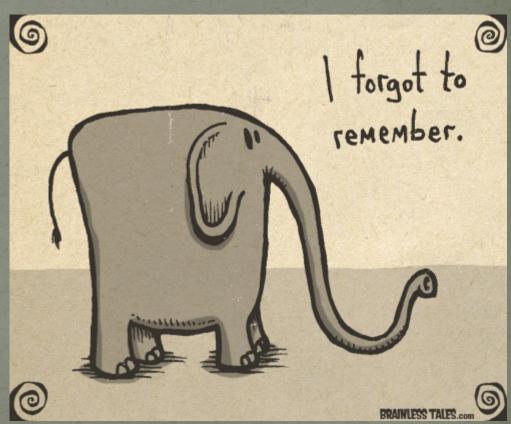
Binary Diffusion Model



Usher-McClelland Model

*Represents decision making using neural populations.

Leaky.



Source: http://www.brainlesstales.com/images/2010/Mar/forgot-remember.jpg

Usher-McClelland Model

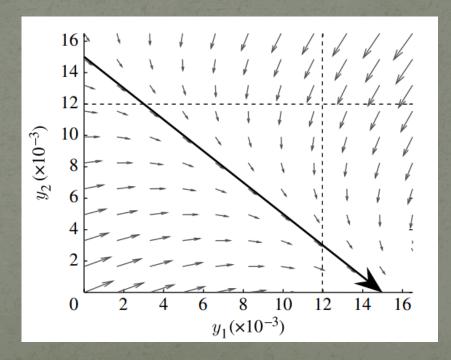
Inhibitory.



Source: http://2.bp.blogspot.com/_walYVfGceg4/ TEDpw1pQ_tl/AAAAAAAAAIs/I1U84iqIcxg/s1600/Sumo +074.JPG

Usher-McClelland Model

When the leak rate and inhibitory rate are equal this model reduces to the diffusion model and is optimal.



Temnothorax albipennis



- Colony size ~100
- Live in Rock crevices

Apis mellifera



- Western honey bee
- < 50000 workers
- Nest in tree cavities

Emigration

- When nest degrades or is destroyed, the colony must emigrate
- Send out scouts
- Quality-dependent requirement
 - Leading to a collective decision

Temnothorax albipennis

- Scouter recruit nest-mates
- Recruiters recruit others after approving of a site
- This leads to positive feedback
- When quorum is reached switch to carrying nest-mates
- Size of quorum affects quality of site

Apis mellifera

Scouts recruit using waggle dance

Positive feedback happens when recruits become recruiters

When a decision is made by quorum the whole swarm moves.

Decision Making in House Hunting

Individuals use only local information

The best site can be selected even if information of it come late in the decision making process

In bees the decision making is separated from the execution of the decision.

Modeling Temnothorax albipennis

Model only decision making up to quorum not execution

Ants switch from uncommitted to committed

Modeling Temnothorax albipennis

Optimal decision making can only be achieved if individuals have global knowledge about alternatives.

Therefore optimal parameterization of the model for house hunting is biologically unrealistic.

Modeling House-Hunting with Indirect Switching in A. Mellifera

$$\begin{cases} \dot{y}_{1} = (n - y_{1} - y_{2})(q_{1} + c\eta_{q1}) - y_{1}(k_{1} + c\eta_{k_{1}}) \\ + y_{1}(n - y_{1} - y_{2})(r'_{1} + c\eta_{r'_{1}}), \end{cases}$$

$$\dot{y}_{2} = (n - y_{1} - y_{2})(q_{2} + c\eta_{q2}) - y_{2}(k_{2} + c\eta_{k_{2}})$$

$$+ y_{2}(n - y_{1} - y_{2})(r'_{2} + c\eta_{r'_{2}}).$$

$$(6.3)$$

- > y: population of recruiters for the two sites.
- > q: rate of spontaneous discovery of alternative sites by uncommitted scouts.
- r: recruitment rate.
- **k**: rate of scouts to become uncommitted.
- > cn: noise that the rates are subject to.

Indirect Switching in A. Mellifera

- This model cannot be made exactly or approximately equivalent to the diffusion model of decision-making.
- A. Mellifera house-hunting with indirect switching is not a statistically optimal decision-making strategy.

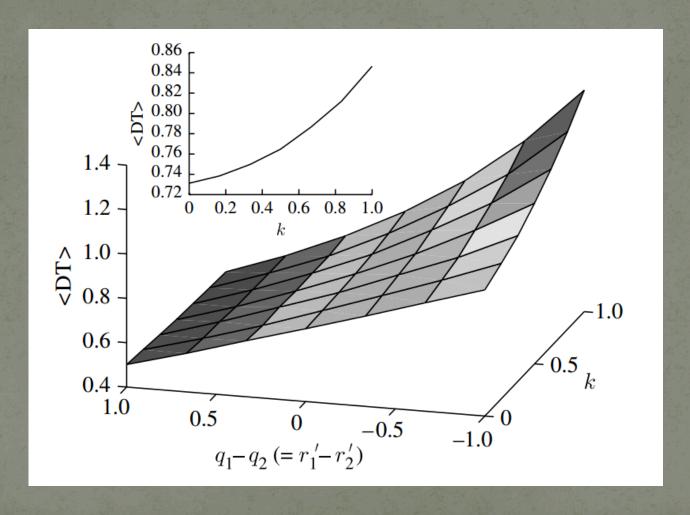
Modeling House-Hunting with Direct Switching in A. Mellifera

$$\begin{cases} \dot{y}_1 = (n - y_1 - y_2)(q_1 + c\eta_{q1}) + y_1(n - y_1 - y_2) \\ \times (r'_1 + c\eta_{r'_1}) - y_1k + y_1y_2(r_1 - r_2 + c\eta_{r1} - c\eta_{r2}), \end{cases}$$

$$\dot{y}_2 = (n - y_1 - y_2)(q_2 + c\eta_{q2}) + y_2(n - y_1 - y_2) \\ \times (r'_2 + c\eta_{r'_2}) - y_2k - y_1y_2(r_1 - r_2 + c\eta_{r1} - c\eta_{r2}).$$

- Similarly, this model cannot be reduced to two independent random processes.
- However x_1 's behavior can be analyzed in the limit when x_2 converges.

House-Hunting with Direct Switching Numerical Simulation



Discussion

- Do you think a standard model of decision making for all biological systems is possible?
- Thoughts on the primate study, confidence?